

(d) The students now decide to use their value for  $g$  to estimate the mass of the Earth.

- (i) Using Newton's universal law of gravitation,  $F = \frac{GMm}{r^2}$ , and  $F = ma$ , show that:

$$M_E = \frac{gR^2}{G} \quad [1]$$

Where  $M_E$  = mass of the Earth

$R$  = Radius of the Earth ( $6.38 \times 10^6 \text{ m} \pm 2\%$ )

$G$  = Gravitational constant ( $6.6743 \pm 0.0007$ )  $\times 10^{-11} \text{ N m}^2 \text{ kg}^{-2}$

•  $mg = \frac{GMm}{r^2}$  *and convincing manipulation (1)*

- (ii) Use the above equation, and your value for  $g$  to estimate the mass of the Earth,  $M_E$ . [1]

- *Mass calculated correctly (e.c.f.) and expressed in kg (1)*

- (iii) Calculate the total **percentage** uncertainty in your answer to (d)(ii). [3]

- *% uncertainty in  $R^2$  given as  $2 \times 2\%$  [=4%]  
[can be awarded by implication if the final answer is correct]*
- *Comment that % uncertainty in  $G$  is irrelevant [or very small]*
- *Total % uncertainty calculated correctly from  $4\% + \%$  uncertainty in  $g$   
[from (c)(ii)] (1)*

- (iv) Hence determine the absolute uncertainty in the mass of the Earth. [2]

- *Absolute uncertainty calculated correctly and expressed to 1 s.f. (1)  
[From (c)(i)  $\times$  (c)(ii) / 100]*
- *mass quoted with a precision consistent with uncertainty (1)*